## Recurrence equations involving different orthogonal polynomial sequences

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Time: Wednesday 24.07., 10:30-11:00, Room SH 02


#### Abstract

Every sequence of real polynomials $\left\{p_{n}\right\}_{n=0}^{\infty}$, orthogonal with respect to a positive weight function $w(x)$ on the interval $(a, b)$, satisfies a three-term recurrence equation. We discuss the role played by the polynomials associated to $p_{n}$, especially as coefficient polynomials in the three-term recurrence equation involving polynomials $p_{n}, p_{n-1}$ and $p_{n-m}, m \in\{2,3, \ldots, n-1\}$. Furthermore, we show how Christoffel's formula is used to obtain mixed three-term recurrence equations involving the polynomials $p_{n}$, $p_{n-1}$ and $g_{n-m, k}, m \in\{2,3, \ldots, n-1\}$, where the sequence $\left\{g_{n, k}\right\}_{n=0}^{\infty}, k \in \mathbb{N}_{0}$, is orthogonal with respect to $c_{k}(x) w(x)>0$ on $(a, b)$ and $c_{k}$ is a polynomial of degree $k$ in $x$. The equations obtained can be used to study the location of the zeros of the appropriate polynomials.


