

# *Logic Programming*

## *Examples*

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# Outline

Repeat

Solving Logic Puzzles

Findall

Graph Search

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Repeat

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# repeat

- ▶ An extra way to generate multiple solutions through backtracking.
- ▶ Comes as a built-in.
- ▶ Easy to define:

```
repeat.  
repeat :- repeat.
```

# repeat

## Effect:

- ▶ If placed in a goal, `repeat` will succeed because of the first fact.
- ▶ If after some time backtracking reaches this point in the goal again, the rule for `repeat` will be tried.
- ▶ The rule generates the goal `repeat`, which will be satisfied by the first fact.
- ▶ If backtracking reaches here again, Prolog will again use the rule it used the fact before.
- ▶ To satisfy the generated `repeat` goal, it will use the fact again, and so on.

```
repeat.  
repeat :- repeat.
```

## How to use repeat

- ▶ `repeat` can be useful to organize an interaction with the user.

```
interact :-  
    repeat,  
        write('Please enter an integer.  
              To stop, type 'stop'.'), nl,  
        read(I),  
        do_something_with_I(I),  
    !.
```

```
do_something_with_I(stop) :-  
    !.
```

```
do_something_with_I(I) :-  
    integer(I),  
    ...  
    !,  
    fail.
```

# Outline

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# Solving Logic Puzzles

- ▶ Logic grid puzzles.
- ▶ Given: The set-up to a scenario and certain clues.
- ▶ Goal: To find an object (e.g. who owns zebra), or to fill in the missing knowledge.
- ▶ Usually given in the form of a grid to be filled in.

	Jam	Marmalade	Honey	Marmite	21	18	15	12	Blue	Green	Yellow	Red
Peter							X					
Jane							X			X		
Simon					X	X	X	X				
Alice								X				
Marmite												
Honey												
Marmalade												
Jam												
12												
15												
18												
21												



# Solving Logic Puzzles

- ▶ Logic grid puzzles can be easily solved by logic programming.
- ▶ Idea: generate-and-test.
- ▶ Generate a possible solution.
- ▶ Test whether it is really a solution (whether it satisfies all the constraints imposed by the puzzle).
- ▶ If yes, finish.
- ▶ If not, generate another possible solution and test again.
- ▶ And so on.

# Solving Logic Puzzles

## Example (From [www.logic-puzzles.org](http://www.logic-puzzles.org))

- ▶ Figure out the reservation, first name, superhero and language for each person using the clues given.
- ▶ Reservations: 5:00pm, 5:30pm, 6:30pm, 7:00pm
- ▶ First Names: Caleb, Emanuel, Johnathan, Karen
- ▶ Superheros: Batman, Hellboy, Iron Man, Spiderman
- ▶ Languages: ASP, Cold Fusion, PHP, Python

# Solving Logic Puzzles

## Example (Cont.)

Clues:

1. The Batman fan is not Caleb.
2. Of Karen and Caleb, one specializes in PHP applications and the other has the 5:30pm reservation.
3. The Hellboy fan has an earlier reservation than the PHP programmer.
4. Emanuel isn't well-versed in Python or Cold Fusion.
5. The person with a reservation at 7:00pm specializes in Cold Fusion applications.
6. The Spiderman fan is Karen.

# Solving Logic Puzzles

## Example (Cont.)

Clues:

7. The ASP programmer doesn't care for Spiderman and is not Karen.
8. Either the Cold Fusion programmer or the PHP programmer collects anything even remotely related to Iron Man.
9. Caleb doesn't care for Iron Man and doesn't have the 6:30pm reservation.
10. The ASP programmer is not Johnathan.
11. The PHP programmer doesn't care for Iron Man.
12. The Spiderman fan has an earlier reservation than the Cold Fusion programmer.

# Solving Logic Puzzles

- ▶ To generate a possible solution, the information about reservations, first names, superheroes, and languages are used.
- ▶ Clues are for testing.
- ▶ The program should follow this structure.

See the [▶ program](#) at the course Web page.

# Outline

Repeat

Solving Logic Puzzles

**Findall**

Graph Search

# Findall

Determine all the terms that satisfy a certain predicate.

`findall(X, Goal, L)`: Succeeds if `L` is the list of all those `X`'s for which `Goal` holds.

## Example

```
?- findall(X, member(X, [a,b,a,c]), L).
```

```
L = [a,b,a,c]
```

```
?- findall(X, member(X, [a,b,a,c]), [a,b,c]).
```

```
false.
```

# More Examples on Findall

## Example

```
?- findall(X, member(5, [a,b,a,c]), L).
```

```
L = []
```

```
?- findall(5, member(X, [a,b,a,c]), L).
```

```
L = [5,5,5,5]
```



# More Examples on Findall

## Example

```
?- findall(5, member(a, [a,b,a,c]), L).
```

```
L = [5,5]
```

```
?- findall(5, member(5, [a,b,a,c]), L).
```

```
L = []
```

# Implementation of Findall

`findall` is a built-in predicate.

However, one can implement it in PROLOG as well:

```
findall(X, G, _) :-
    asserta(found(mark)),
    call(G),
    asserta(found(X)),
    fail.

findall(_, _, L) :-
    collect_found([], M),
    !,
    L=M.

collect_found(S, L) :-
    getnext(X),
    !,
    collect_found([X|S], L).

collect_found(L, L).

getnext(X) :-
    retract(found(X)),
    !,
    X \== mark.
```

## Sample Runs

```
?- findall(X, member(X, [a,b,c]), L).
```

```
L = [a,b,c]
```

```
?- findall(X, append(X,Y,[a,b,c]), L).
```

```
L = [[],[a],[a,b],[a,b,c]]
```

```
?- findall([X,Y], append(X,Y,[a,b,c]), L).
```

```
L = [[],[a,b,c], [[a],[b,c]], [[a,b],[c]],  
[[a,b,c],[]]]
```

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# Representing Graphs

$a(g, h)$  .

$a(g, d)$  .

$a(e, d)$  .

$a(h, f)$  .

$a(e, f)$  .

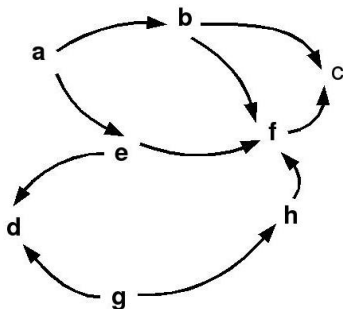
$a(a, e)$  .

$a(a, b)$  .

$a(b, f)$  .

$a(b, c)$  .

$a(f, c)$  .



# Moving Through Graph

Simple program for searching the graph:

- ▶ `go (X, X) .`  
`go (X, Y) :- a (X, Z) , go (Z, Y) .`
- ▶ Drawback: For cyclic graphs it will loop.
- ▶ Solution: Keep track of nodes visited.

# Improved Program for Graph Searching

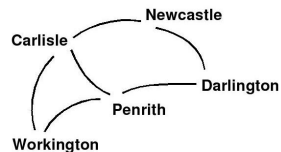
`go(X, Y, T)` : Succeeds if one can go from node `X` to node `Y`.  
`T` contains the list of nodes visited so far.

```
go(X, X, T) .  
go(X, Y, T) :-  
    a(X, Z),  
    legal(Z, T),  
    go(Z, Y, [Z|T]).
```

```
legal(X, []).  
legal(X, [H|T]) :-  
    X \= H,  
    legal(X, T).
```

# Car Routes

```
a(newcastle, carlisle).  
a(carlisle, penrith).  
a(darlington, newcastle).  
a(penrith, darlington).  
a(workington, carlisle).  
a(workington, penrith).
```





# Car Routes Program

```
go(Start, Dest, Route) :-  
    go0(Start, Dest, [], R),  
    reverse(R, Route).
```

```
go0(X, X, T, [X|T]).  
go0(Place, Dest, T, Route) :-  
    legalnode(Place, T, Next),  
    go0(Next, Dest, [Place|T], Route).
```

## Car Routes Program, Cont.

```
legalnode(X, Trail, Y) :-  
    (a(X, Y) ; a(Y, X)),  
    legal(Y, Trail).
```

```
legal(_, []).  
legal(X, [H|T]) :-  
    X \= H,  
    legal(X, T).
```

```
reverse(L1, L2) :- reverse(L1, [], L2).
```

```
reverse([X|L], L2, L3) :-  
    reverse(L, [X|L2], L3).  
reverse([], L, L).
```

# Runs

```
?- go(darlington, workington, X).  
X = [darlington,newcastle,carlisle,  
     penrith,workington];  
X = [darlington,newcastle,carlisle,  
     workington];  
X = [darlington,penrith,carlisle,workington];  
X = [darlington,penrith,workington];  
false.
```

# Deficiencies of the Program

- ▶ Can not survey the complete list of possibilities.
- ▶ Remained options are implicit in the backtracking structure of Prolog.
- ▶ They are not explicit in the structure that the program examines.

# Deficiencies of the Program

- ▶ Can not survey the complete list of possibilities.
- ▶ Remained options are implicit in the backtracking structure of Prolog.
- ▶ They are not explicit in the structure that the program examines.
- ▶ We try to come up with a more general-purpose solution.

# Findall Paths

```
go(Start, Dest, Route) :-  
    go1([[Start]], Dest, R),  
    reverse(R, Route).  
  
go1([First|Rest], Dest, First) :-  
    First = [Dest|_].  
go1([[Last|Trail]|Others], Dest, Route) :-  
    findall([Z,Last|Trail],  
           legalnode(Last, Trail, Z),  
           List),  
    append(List, Others, NewRoutes),  
    go1(NewRoutes, Dest, Route).
```

# Depth First

```
?- go(darlington, workington, X).
```

```
X = [darlington,newcastle,  
      carlisle,penrith,workington];
```

```
X = [darlington,newcastle,  
      carlisle,workington];
```

```
X = [darlington,penrith,  
      carlisle,workington];
```

```
X = [darlington,penrith,workington];
```

```
false.
```

## Depth, Breadth First

```
go1 ([[Last|Trail]|Others], Dest, Route) :-  
    findall([Z,Last|Trail],  
           legalnode(Last, Trail, Z),  
           List),  
    append(List, Others, NewRoutes),  
    go1(NewRoutes, Dest, Route).
```

```
go1 ([[Last|Trail]|Others], Dest, Route) :-  
    findall([Z,Last|Trail],  
           legalnode(Last, Trail, Z),  
           List),  
    append(Others, List, NewRoutes),  
    go1(NewRoutes, Dest, Route).
```



# Breadth First

```
?- go(darlington,workington,X).  
X = [darlington,penrith,workington];  
X = [darlington,newcastle,  
     carlisle,workington];  
X = [darlington,penrith,  
     carlisle,workington];  
X = [darlington,newcastle,  
     carlisle,penrith,workington];  
false.
```